

α -MATHEMATICS

Alpha Wiskunde Graad 10 / *Alpha Mathematics Grade 10*

Finale Eksamen 2023 / *Final Examination 2023*

MEMORANDUM

Totaal / *Total*: 120 punte / *marks*

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Moderator: Rika Grobler

Hierdie memorandum bestaan uit 8 bladsye. /

This memorandum consists of 8 pages.

Vraag / Question 1**[20 punte / marks]**

1.1	A	B	C	D
1.2	A	B	C	D
1.3	A	B	C	D
1.4	A	B	C	D
1.5	A	B	C	D
1.6	A	B	C	D
1.7	A	B	C	D
1.8	A	B	C	D
1.9	A	B	C	D
1.10	A	B	C	D

Vraag / Question 2

[16 punte / marks]

NR. NO	ANTWOORD / ANSWER	PUNTE / MARKS
2.1	$a + b$ $= 6 + 3i$ ✓✓	(2)
2.2	$2a \cdot 3b$ $= 2(2 - 3i) \cdot 3(4 + 6i)$ ✓ $= (4 - 6i)(12 + 18i)$ ✓ $= 48 + 72i - 72i - 108i^2$ ✓ $= 156$ ✓	(4)
2.3	$i^{51} \cdot a^2 b$ $= -i(2 - 3i)^2(4 + 6i)$ ✓ $= -i(4 - 12i + 9)(4 + 6i)$ ✓ $= -i(-5 - 12i)(4 + 6i)$ $= -i(-20 - 30i - 48i + 72)$ ✓ $= 20i + 30i^2 + 48i^2 - 72i$ $= -78 - 52i$ ✓✓	(5)
2.4	$\frac{a}{b}$ $= \frac{2 - 3i}{4 + 6i} \times \frac{4 - 6i}{4 - 6i}$ ✓ $= \frac{-10 - 24i}{16 - 36i^2}$ ✓ $= \frac{-10 - 24i}{16 + 36}$ ✓ $= -\frac{5}{26} - \frac{6}{13}i$ ✓	(5)

Vraag / Question 3

[12 punte / marks]

ANTWOORD / ANSWER	PUNTE / MARKS
$\frac{-8x - 20}{(x^2 - 4)(x + 1)} = \frac{-8x}{(x + 2)(x - 2)(x + 1)} \checkmark = \frac{A}{x + 2} + \frac{B}{x - 2} + \frac{C}{x + 1} \checkmark$ $-8x - 20 = A(x - 2)(x + 1) + B(x + 2)(x + 1) + C(x + 2)(x - 2) \checkmark$ <p> $x = 2 \checkmark$ $-36 = 12B$ $B = -3 \checkmark$ </p> <p> $x = -2 \checkmark$ $-4 = 4A$ $A = -1 \checkmark$ </p> <p> $x = -1 \checkmark$ $-12 = -3C$ $C = 4 \checkmark$ </p> $\frac{-8x - 20}{(x^2 - 4)(x + 1)} = \frac{-1}{x + 2} \checkmark - \frac{3}{x - 2} \checkmark + \frac{4}{x + 1} \checkmark$	<p>(12)</p>

Vraag / Question 4

[11 punte / marks]

NR. NO	ANTWOORD / ANSWER	PUNTE / MARKS
	$2x - y + 3z = 6$ $4x - 2y + z = 1$ $x + y + z = 3$ $\begin{bmatrix} 2 & -1 & 3 \\ 4 & -2 & 1 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 1 \\ 3 \end{bmatrix} \checkmark\checkmark$ $\begin{vmatrix} 2 & -1 & 3 \\ 4 & -2 & 1 \\ 1 & 1 & 1 \end{vmatrix} = 2 \begin{vmatrix} -2 & 1 \\ 1 & 1 \end{vmatrix} + \begin{vmatrix} 4 & 1 \\ 1 & 1 \end{vmatrix} + 3 \begin{vmatrix} 4 & -2 \\ 1 & 1 \end{vmatrix} \checkmark$ $= 2(-2 - 1) + (4 - 1) + 3(4 + 2) \checkmark$ $= 15 \checkmark\checkmark$ $\begin{vmatrix} 6 & -1 & 3 \\ 1 & -2 & 1 \\ 3 & 1 & 1 \end{vmatrix} = 6 \begin{vmatrix} -2 & 1 \\ 1 & 1 \end{vmatrix} + \begin{vmatrix} 1 & 1 \\ 3 & 1 \end{vmatrix} + 3 \begin{vmatrix} 1 & -2 \\ 3 & 1 \end{vmatrix} \checkmark$ $= 6(-2 - 1) + (1 - 3) + 3(1 + 6) \checkmark$ $= 1 \checkmark\checkmark$ $x = \frac{1}{15} \checkmark$	

Vraag / Question 5

[18 punte / marks]

NR. NO	ANTWOORD / ANSWER	PUNTE / MARKS
5.1.1	$ a = \sqrt{3^2 + 8^2} \checkmark = \sqrt{73} \checkmark$ Unit vector is: $\left(\frac{3}{\sqrt{73}}; \frac{8}{\sqrt{73}}\right) \checkmark$	(3)
5.1.2	$a \cdot b = -5 \checkmark$ $-5 \checkmark = \sqrt{73} \cdot \sqrt{2} \cos \theta \checkmark$ $\theta \approx 2 \checkmark \checkmark$	(5)
5.2.1	$v \cdot u = 0 \checkmark \checkmark$	(2)
5.2.2	The vectors are perpendicular. / Die vektore is loodreg op mekaar. $\checkmark \checkmark$	(2)
5.2.3	$\frac{\pi}{2} \checkmark \checkmark$	(2)
5.2.4	$6v + 2u$ $= (-84; -84) \checkmark + (4; -4) \checkmark$ $= (-80; -88) \checkmark \checkmark$	(4)

Vraag / Question 6

[20 punte / marks]

NR. NO	ANTWOORD / ANSWER	PUNTE / MARKS
6.1		(7) One mark for each end point $\checkmark \checkmark \checkmark \checkmark \checkmark$ One mark for shape $\checkmark \checkmark$

6.2	$F(x) = \frac{2}{x+1} - \sqrt[3]{2+x-1} + x + 1$ $f(x) = \frac{2}{x} - \sqrt[3]{x} + x \checkmark \checkmark$ $g(x) = x + 1 \checkmark$	(3)
6.3.1	$(f \circ g)(x) = 2(\sqrt{x^2+9})^2 \checkmark - \sqrt{x^2+9} \checkmark + 1 \checkmark$ $= 2x^2 + 19 - \sqrt{x^2+9} \checkmark$	(4)
6.3.2	$(f \circ g)(-4) = 2(-4)^2 + 19 - \sqrt{(-4)^2+9} \checkmark$ $= 46 \checkmark$	(2)
6.3.3	$(g \circ f)(x) = \sqrt{(2x^2 - x + 1)^2 + 9} \checkmark \checkmark$	(2)
6.3.4	$(f \circ f)(x) = 2(2x^2 - x + 1)^2 - (2x^2 - x + 1) + 1 \checkmark \checkmark$	(2)

Vraag / Question 7

[14 punte / marks]

NR. NO	ANTWOORD / ANSWER	PUNTE / MARKS
7.1.1	$f'(x) = 15x^4 \checkmark - 21x^2 \checkmark + \frac{1}{2}x^{-\frac{3}{2}} \checkmark + 25x^{-6} \checkmark$	(4)
7.1.2	$\int (3x^5 - 7x^3 + 2x^{\frac{1}{4}} - 5x^{-5} \checkmark) dx$ $= \frac{x^6 \checkmark}{2} - \frac{7x^4 \checkmark}{4} + \frac{8x^{\frac{5}{4}} \checkmark}{5} + \frac{5x^{-4} \checkmark}{4} + c$	(5)
7.2	$V = \pi \int_0^3 [(2x+3)^4]^2 dx$ $= \pi \int_0^3 (2x+3)^8 dx \checkmark$ $= \pi \left(\frac{(2x+3)^9}{9(2)} \right) \Big _0^3 \checkmark \checkmark$ $= 67\,614\,195,9 \text{ units}^2 \checkmark \checkmark$	(5)

Vraag / Question 8

[9 punte / marks]

NR. NO	ANTWOORD / ANSWER	PUNTE / MARKS
8.1	$f(-2) = 0$ $x = -2$ ✓✓	(2)
8.2	$(x + 2)$ ✓✓	(2)
8.3	$ \begin{array}{r} x^2 \quad +x \quad -12 \\ \hline x^3 \quad 3x^2 \quad -10x \quad -24 \\ -x^3 \quad -2x^2 \\ \hline \quad x^2 \quad -10x \quad -24 \\ \quad -x^2 \quad -2x \\ \hline \quad -12x \quad -24 \\ \quad 12x \quad +24 \\ \hline \quad 0 \end{array} $ $x^2 + x - 12$ ✓✓✓	(3)
8.4	$(x + 2)(x^2 + x - 12) = 0$ $(x + 2)(x + 4)(x - 3) = 0$ ✓ $x = -4 ; -2 ; 3$ ✓	(2)

- EINDE VAN DIE MEMORANDUM / END OF THE MEMORANDUM -